

7239

BOARD DIPLOMA EXAMINATION, (C-20) OCTOBER/NOVEMBER—2023

DECE - THIRD SEMESTER (COMMON) EXAMINATION

ENGINEERING MATHEMATICS—II

Time: 3 Hours [Total Marks: 80

PART—A

 $3 \times 10 = 30$

Instructions: (1) Answer **all** questions.

(2) Each question carries three marks.

1. Evaluate
$$\int x^9 + \cos x + e^x dx$$

2. Evaluate
$$\int \frac{3}{x} + 3^x + x^3 dx$$

3. Evaluate
$$\int \frac{\sec^2(\log x)}{x} dx$$

4. Evaluate
$$\int x^3 \log x \ dx$$

5. Evaluate
$$\int_0^1 (x-2)(x+3) dx$$

- **6.** Find the area of the region bounded by $y^2 = 4x$ between x = 0 and x = 3.
- **7.** Find the mean value of $y = x e^x$ on [0, 1].
- **8.** Form the differential equation by eliminating the arbitrary constants A, B from the equation $y = A \cos 5x + B \sin 5x$.

- **9.** Solve $\frac{dy}{dx} = e^{x-y}$
- **10.** Find the integrating factor of $\frac{dy}{dx} + y \cot x = \cos ex$.

PART—B 8×5=40

Instructions: (1) Answer **all** questions.

(2) Each question carries eight marks.

11. (a) Evaluate $\int \sin^5 x \cdot \cos^3 x \ dx$

(OR)

(b) Evaluate
$$\int \frac{1}{x^2 + 8x + 20} dx$$

12. (a) Evaluate $\int \frac{x}{(x-7)(x-5)} dx$

(OR)

(b) Evaluate
$$\int x \cdot \sin 2x \cdot \cos x \, dx$$

13. (a) Evaluate $\int_0^1 x(1-x)^7 dx$

(OR)

- (b) Evaluate $\int_0^{\frac{\pi}{2}} \frac{1}{1 + \cot x} dx$
- **14.** (a) Find the area bounded by $y^2 = 8x$ and the line 2x y 8 = 0.

(OR)

- (b) Find the RMS value of $y = x^2 + 2$ on [0, 2].
- **15.** (a) Find the volume generated by revolution of $\frac{x^2}{64} + \frac{y^2}{16} = 1$ about X-axis.

(OR)

(b) Evaluate $\int_{1}^{2} \frac{1}{x} dx$ approximately by using Simpson's rule by dividing [1, 2] into 10 equal parts.

PART—C 10×1=10

Instructions: (1) Answer the following question.

- (2) The question carries **ten** marks.
- **16.** Solve $(y^2 xy) dx = x^2 dy$
